

The equation is the same as previous problem. Only difference is, the elastic tensor  $D_{ijkl}$  is a function of  $\eta$  now.

$$\sigma_{ij,i} = 0$$

in which

$$\begin{aligned}\sigma_{ij} &= D_{ijkl}\epsilon_{kl}^{ela} \\ &= \left( \frac{\eta_{\gamma'} - \eta}{\eta_{\gamma'} - \eta_{\gamma}} D_{ijkl}^{\gamma} + \frac{\eta - \eta_{\gamma}}{\eta_{\gamma'} - \eta_{\gamma}} D_{ijkl}^{\gamma'} \right) (\epsilon_{kl} - \epsilon_{kl}^0) \\ &= \left( \frac{\eta_{\gamma'} - \eta}{\eta_{\gamma'} - \eta_{\gamma}} D_{ijkl}^{\gamma} + \frac{\eta - \eta_{\gamma}}{\eta_{\gamma'} - \eta_{\gamma}} D_{ijkl}^{\gamma'} \right) \left[ \frac{1}{2} \left( \frac{\partial u_k}{\partial x_l} + \frac{\partial u_l}{\partial x_k} \right) - \eta \epsilon_{kl}^{00} \right]\end{aligned}$$

where

$\eta_{\gamma'}$  and  $\eta_{\gamma}$  are constant scalars(numbers).  $\eta$  is actually  $\eta = \eta(\vec{r})$  a scalar field.  
 $D_{ijkl}^{\gamma'}$  and  $D_{ijkl}^{\gamma}$  are constant elastic tensors.  $\epsilon_{kl}^{00}$  is constant strain tensor.