

Elegant String Searches

Martin Schweitzer

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The Problem

Given a set of letters and a dictionary, find all words that can be made from those letters.

H	C	O
C	A	L
E	T	O

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The naive approach

- ▶ Find all 9-letter permutations

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- ▶ Check each permutation against every word in dictionary

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- ▶ Find all 9-letter permutations
- ▶ Check each permutation against every word in dictionary
- ▶ Find all 8-letter permutations

The naiive approach

- ▶ Find all 9-letter permutations
- ▶ Check each permutation against every word in dictionary
- ▶ Find all 8-letter permutations
- ▶ Check each permutation against every word in dictionary

The naiive approach

- ▶ Find all 9-letter permutations
- ▶ Check each permutation against every word in dictionary
- ▶ Find all 8-letter permutations
- ▶ Check each permutation against every word in dictionary
- ▶ Find all 7-letter permutations

The naiive approach

- ▶ Find all 9-letter permutations
- ▶ Check each permutation against every word in dictionary
- ▶ Find all 8-letter permutations
- ▶ Check each permutation against every word in dictionary
- ▶ Find all 7-letter permutations
- ▶ ...

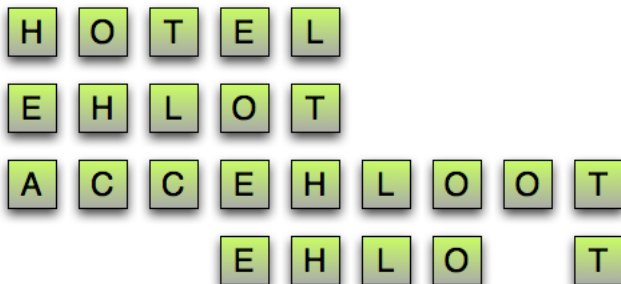
The Experienced approach

- ▶ Sort the letters in the square

H	O	T	E	L					
E	H	L	O	T					
A	C	C	E	H	L	O	O	T	
			E	H	L	O			T

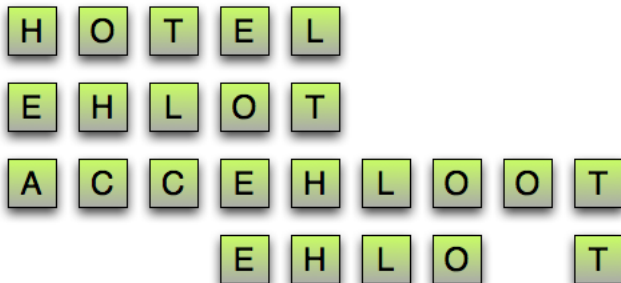
The Experienced approach

- ▶ Sort the letters in the square
- ▶ For each word in the dictionary



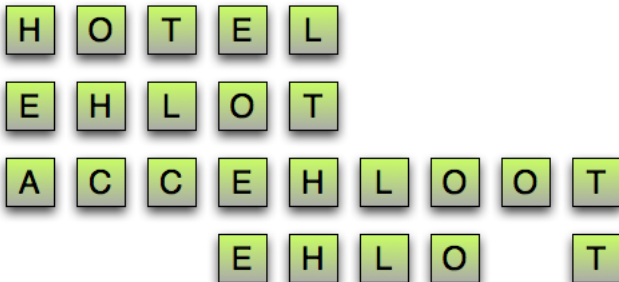
The Experienced approach

- ▶ Sort the letters in the square
- ▶ For each word in the dictionary
 - ▶ sort the word



The Experienced approach

- ▶ Sort the letters in the square
- ▶ For each word in the dictionary
 - ▶ sort the word
 - ▶ check if we can make that word



The Experienced approach

- ▶ Only go through the dictionary once

The Experienced approach

- ▶ Only go through the dictionary once
- ▶ Still have to sort each word in the dictionary

The Fundamental Theorem of Arithmetic

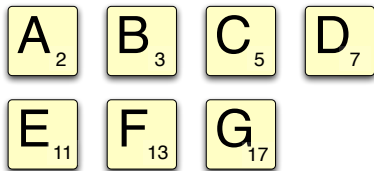
Every natural number greater than 1 can be written as a unique product of prime numbers

$$6939 = 2^3 \times 3 \times 17^2$$

$$1200 = 2^4 \times 3 \times 5^2$$

$$36 = 2^2 \times 3^2$$

Fundamental insight



Fundamental insight

$$\begin{array}{cccc} \boxed{A_2} & \boxed{B_3} & \boxed{C_5} & \boxed{D_7} \\ \boxed{E_{11}} & \boxed{F_{13}} & \boxed{G_{17}} & \\ \boxed{A_2} & \boxed{B_3} & \boxed{B_3} & \boxed{A_2} = 36 \end{array}$$

Fundamental insight

A₂ B₃ C₅ D₇

E₁₁ F₁₃ G₁₇

A₂ B₃ B₃ A₂ = 36

B₃ A₂ B₃ A₂ = 36

Fundamental insight

A₂ B₃ C₅ D₇

E₁₁ F₁₃ G₁₇

A₂ B₃ B₃ A₂ = 36

B₃ A₂ B₃ A₂ = 36

B₃ A₂ B₃ = 18

Fundamental insight

A₂ B₃ C₅ D₇

E₁₁ F₁₃ G₁₇

A₂ B₃ B₃ A₂ = 36

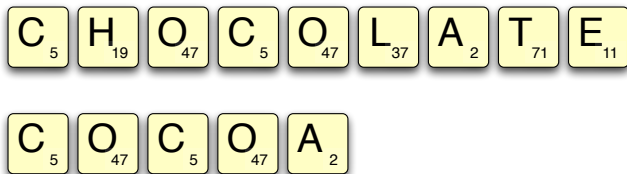
B₃ A₂ B₃ A₂ = 36

B₃ A₂ D₇ = 42

Does chocolate contain cocoa?

C₅ H₁₉ O₄₇ C₅ O₄₇ L₃₇ A₂ T₇₁ E₁₁

Does chocolate contain cocoa?



Does chocolate contain cocoa?

C₅ H₁₉ O₄₇ C₅ O₄₇ L₃₇ A₂ T₇₁ E₁₁

C₅ O₄₇ C₅ O₄₇ A₂

```
»» print 5 * 19 * 47 * 5 * 47 * 37 * 2 * 71 * 11
```


Does chocolate contain cocoa?

C₅ H₁₉ O₄₇ C₅ O₄₇ L₃₇ A₂ T₇₁ E₁₁

C₅ O₄₇ C₅ O₄₇ A₂

```
>>> print 5 * 19 * 47 * 5 * 47 * 37 * 2 * 71 * 11  
60641799350
```

Does chocolate contain cocoa?

C₅ H₁₉ O₄₇ C₅ O₄₇ L₃₇ A₂ T₇₁ E₁₁

C₅ O₄₇ C₅ O₄₇ A₂

```
>>> print 5 * 19 * 47 * 5 * 47 * 37 * 2 * 71 * 11  
60641799350
```

```
>>> print 5 * 47 * 5 * 47 * 2
```

Does chocolate contain cocoa?

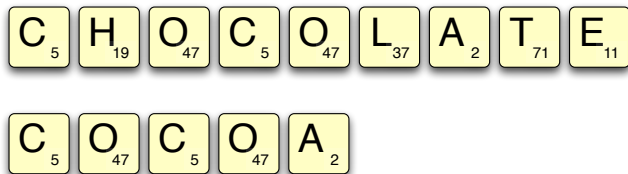
C₅ H₁₉ O₄₇ C₅ O₄₇ L₃₇ A₂ T₇₁ E₁₁

C₅ O₄₇ C₅ O₄₇ A₂

```
>>> print 5 * 19 * 47 * 5 * 47 * 37 * 2 * 71 * 11  
60641799350
```

```
>>> print 5 * 47 * 5 * 47 * 2  
110450
```

Does chocolate contain cocoa?

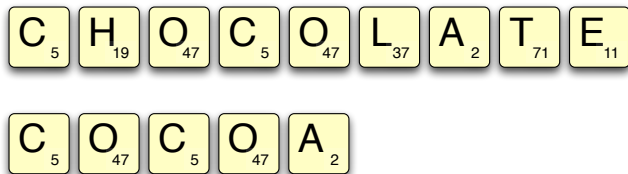


```
>>> print 5 * 19 * 47 * 5 * 47 * 37 * 2 * 71 * 11  
60641799350
```

```
>>> print 5 * 47 * 5 * 47 * 2  
110450
```

```
>>> print 60641799350 % 110450
```

Does chocolate contain cocoa?



```
>>> print 5 * 19 * 47 * 5 * 47 * 37 * 2 * 71 * 11  
60641799350
```

```
>>> print 5 * 47 * 5 * 47 * 2  
110450
```

```
>>> print 60641799350 % 110450  
0
```

```
primes = [2, 3, 5, 7, 11, 17, ...
```

```
def find_number(word):  
    tot = 1  
    for ch in word:  
        tot = tot * primes[ord(ch.lower()) - ord('a')]  
    return tot
```

Program 1

```
#!/usr/bin/python
dictionary = '/usr/share/dict/words'
secret = 'chocolate'
primes = [2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31,

def prime_val(ch):
    return primes[ord(ch.lower()) - ord('a')]

def get_val(word):
    total = 1
    for ch in word:
        total *= prime_val(ch)
    return total
```

Program 1 (continued)

```
magic = get_val(secret)
for word in open(dictionary):
    word = word.rstrip('\n')
    if magic % get_val(word) == 0:
        print word
```


The following lines:

```
def get_val(word):  
    total = 1  
    for ch in word:  
        total *= prime_val(ch)  
    return total
```

Can be replaced by:

```
def get_val(word):  
    return reduce(lambda x,y: x*y, map(lambda x:  
        primes[ord(x) - ord('a')], word.lower()))
```

Program 2

```
dictionary = '/usr/share/dict/words'  
secret = 'chocolate'  
primes = [2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31,  
  
def get_val(word):  
    return reduce(lambda x,y: x*y, map(lambda x:  
        primes[ord(x) - ord('a')], word.lower()))  
  
magic = get_val(secret)  
for word in open(dictionary):  
    word = word.rstrip('\n')  
    if magic % get_val(word) == 0:  
        print word
```

List comprehension

The following code:

```
def get_val(word):  
    return reduce(lambda x,y: x*y, map(lambda x:  
        primes[ord(x) - ord('a')], word.lower()))
```

Can be (and should be?) replaced with:

```
def get_val(word):  
    return [j for j in [1] for i in word for j in  
        [j * primes[ord(i.lower()) - ord('a')]]][:-1]
```

More reductions

And the following code:

```
for word in open(dictionary):
    word = word.rstrip('\n')
    if magic % get_val(word) == 0:
        print word
```

Can be replaced with:

```
[print3(word.strip()) for word in open(dictionary)
    if magic % get_val(word.rstrip('\n')) == 0]
```

Program 3

```
dictionary = '/usr/share/dict/words'  
secret = 'chocolate'  
primes = [2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31,  
  
def get_val(word):  
    return [j for j in [1] for i in word for j in  
            [j * primes[ord(i.lower()) - ord('a')]]][-1]  
  
def print3(word): print word  
  
magic = get_val(secret)  
[print3(word.strip()) for word in open(dictionary)  
    if magic % get_val(word.rstrip('\n')) == 0]
```

- ▶ The first solution is not necessarily the best.

Conclusions

- ▶ The first solution is not necessarily the best.
- ▶ Python rocks.

- ▶ The first solution is not necessarily the best.
- ▶ Python rocks.
- ▶ Sometimes something that they taught you in school is useful.

T₇₁ H₁₉ E₁₁
N₄₁
D₇